

Basic Aspects of Mechanical Stability of Tree Cross-Sections

By Frank Rimm

The mechanical stability of a tree trunk against bending loads caused by wind depends on the strength and condition of its wood as well as on the size and shape of its cross-section. A basic understanding of these aspects can help when evaluating tree strength loss due to decay within the scope of tree risk assessments.

Diameter and Stability

When a tree is impacted by a wind force, its cells in the trunk on the windward (wind-exposed) side are stretched, while those on the leeward (wind-sheltered) side are compressed (Figure 1).

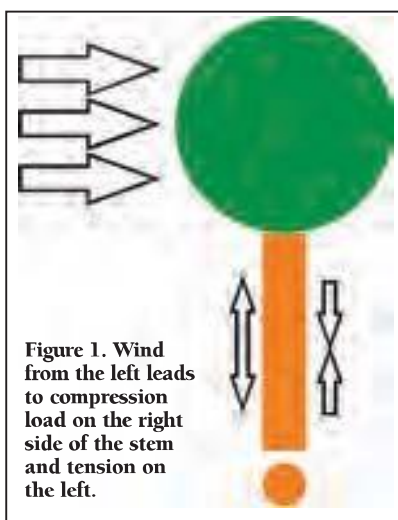


Figure 1. Wind from the left leads to compression load on the right side of the stem and tension on the left.

Furthermore, the tree crown's own weight has to be added as well, which results in an even higher compression load on the leeward cells and a correspondingly lower tension on the opposite side.

To describe the tree's ability to withstand such bending loads, the so-called "moment of resistance," represented by the symbol "W" (for the German word *Widerstandsmoment*) is used. It characterizes the mech-

anical stability of a cross-section as far as it depends on size and geometrical shape. The resistance moment of a circular cross-section with a diameter D can be summarized with a simple formula:

$$W = Pi \cdot \frac{D^4}{32}$$

This formula helps us understand the effect of diameter on stability: if the diameter is doubled, for instance, the moment of resistance increases eightfold, since $(2D)^4 = 8D^4$. Likewise, if trunk diameter grows one percent, its moment of resistance rises by about three percent, since $(1.01D)^4 \approx 1.03D^4$. Therefore, an annual tree growth ring width of 0.2 in (5 mm) within a tree trunk cross-section of 20 in (500 mm) diameter (so one percent increase on each side) denotes a stabilization of a tree trunk cross-section of about 6 percent. In this manner, a sound tree gains stability by its annual ring growth on a yearly basis, ignoring potential changes in the tree crown's surface or wind load and internal damages.

Wrapped Curves Around Cross-Sections

To precisely calculate the load-carrying capacity of a tree trunk cross-section, often called its "strength" or "stability," one would have to know the individual characteristics of each cell and the stability

of its compounds. This is hardly feasible, neither in terms of practical work with trees nor with scientific measurement. Therefore, it seems appropriate to adopt a simpler and more relative approach.

We can do this by calculating the moment of resistance for loading capacities from 1° to 360° (all wind directions), then dividing each result by the maximal value to produce a relative stability percentage. Those numbers would normally be represented as a linear graph, with the x-axis representing wind direction and the y-axis the percentage of maximum strength/stability. For better understanding, we can also wrap such a graph around the trunk cross-section to better visualize this effect. A circular trunk cross-section shows, therefore, a constant

stability towards wind loads from all directions. Consequently, the curve of the calculated relative stability percentages (moment of resistance) runs along the 100 percent level, creating a perfect circle on the wrapped graph (Figure 2).

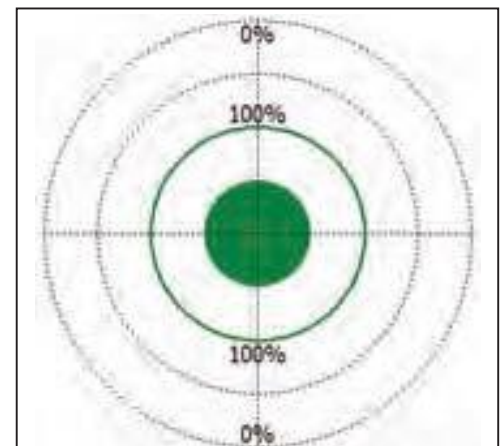


Figure 2. The green curve indicates relative strength of the cross-section against wind load as revealed by the moment of resistance.

Influence of Trunk Profile

This situation changes with different cross-sectional shapes. Trees growing between buildings that are located on their northern and southern side (so wind load is limited to the west or east), for example, mostly develop oval trunk cross-sections (Figure 3). In such a case, calculation of relative stability reveals the consequences of this mechanical impact on tree growth: a tree trunk with an E-W diameter of 40 in (1 m) and a N-S diameter of 28 in (0.7 m)

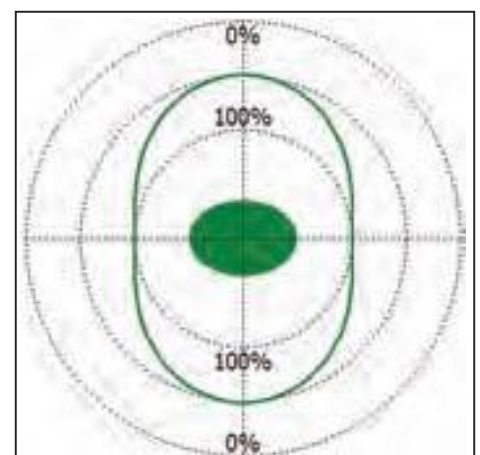


Figure 3. The weaker the cross section the more the green curve bulges into the direction of the corresponding wind flow.

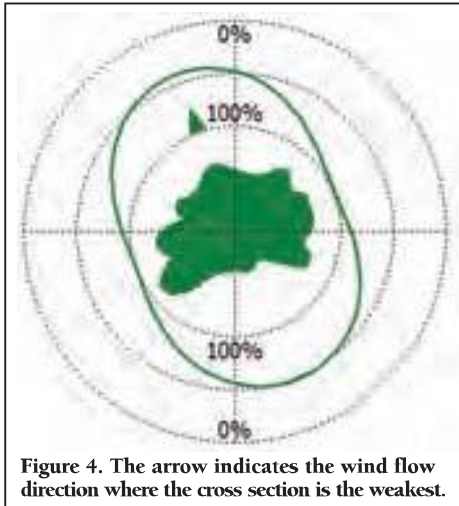


Figure 4. The arrow indicates the wind flow direction where the cross section is the weakest.

retains only approx. 50 percent of maximum stability when exposed to wind load from the north or south. The relative stability curve around the trunk “bulges” accordingly (Figure 3), where the bulges represent drops in strength. As a consequence, if the buildings south of the tree were demolished and

the tree suddenly exposed to wind from that direction, the possibility of the tree’s failure would be greatly increased.

Trunk flares at the lower trunk cannot only be used to estimate the primary wind-loading direction. In addition, they are critical for a tree’s stability because of their influence on the profile of the cross-section.

For example, the cross-section in Figure 4 matches a tree growing at a location where the dominant wind exposure is to the south-west. Along the SW-NE axis of wind exposure, the resulting cross-section is approximately twice as strong along the opposing SE-NW axis.

The green arrow pointing SE on the diagram indicates that the cross-section displays the lowest stability against wind loading from the NW, as revealed by the large bulge (=drop in strength) on the opposite side. If the tree were exposed to wind loads from all directions, the highest possibility of a bending break would be expected in the direction of the arrow.

Defect Size and Strength Loss

In the simple case of a circular trunk cross-section with a cavity in its center, the internal diameter of this cavity will be included in calculating the moment of resistance:

$$W = P_i \cdot \frac{D^4 - d^4}{32 \cdot D}$$

For example, a trunk diameter of $D=40$ in (1 m) with a center cavity diameter $d=20$ in (0.5 m) has 50 percent of its radius missing. That corresponds to a loss of cross-section surface of 25 percent but a relative strength loss of a mere 6 percent. Following this equation, when about 70 percent of the radius is gone (i.e., $t/R \approx 0.3$), the cross-section lost about 50 percent of its area but only 25 percent of its strength (Figure 5).

Consequently, the actual strength loss is significantly lower than professionals as well as laymen might expect when observing the extent of internal damage. If this aspect is considered when making decisions about tree stability, it can often save the tree, especially if non-arborists have to decide what action has to be taken – be it neighbours in dispute or politicians.

As the cross-sectional residual wall (‘shell wall’) continues to thin out (Figure 6), the informational value of the formula we examined begins to reach the limits of its validity: it assumes that a cross-section stays firm and does not get deformed due to the loading force. But, the

torsional and shear strength characteristics of wood are significantly lower compared to compression and tension strength in longitudinal direction. Skatter and Kucera (2000) showed that this is the reason why torsion is an important factor for tree failures.

For example, a tree trunk with a remaining shell wall thickness of only 10 percent of the radius (Figure 7), should theoretically still provide 35 percent of its strength. This cannot be true and needs to be corrected due to torsional effects, shear stresses and different failure modes than just bending.

Influence of Location of Decay

Up to this point we have assumed that the decay was located in the center of the cross-section. When it is not, different calculations must be used: mathematically speaking, an integral is calculated summarizing the contribution of each wooden cell regarding whether it is loaded under compression or tension.

When wood decay in a tree trunk is at the edge, the resistance moment towards the opposite side from the decay decreases to a greater degree because tension strength of wood is higher than compression strength (FPL 2010).

Figure 8 represents such an off-center situation, characterized in this example by a thin or missing shell wall on one side. As earlier, the red curve shows the relative value of resistance moment in the

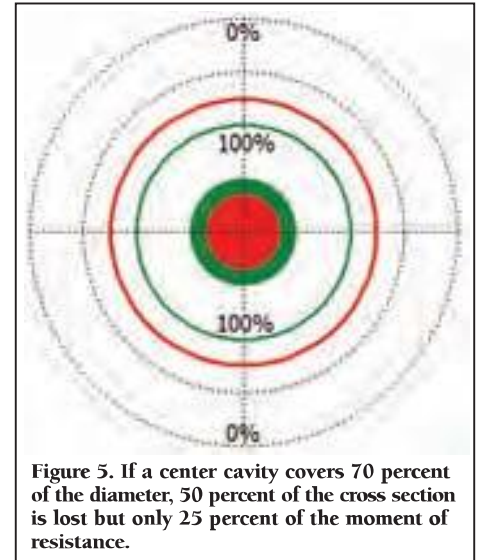


Figure 5. If a center cavity covers 70 percent of the diameter, 50 percent of the cross section is lost but only 25 percent of the moment of resistance.

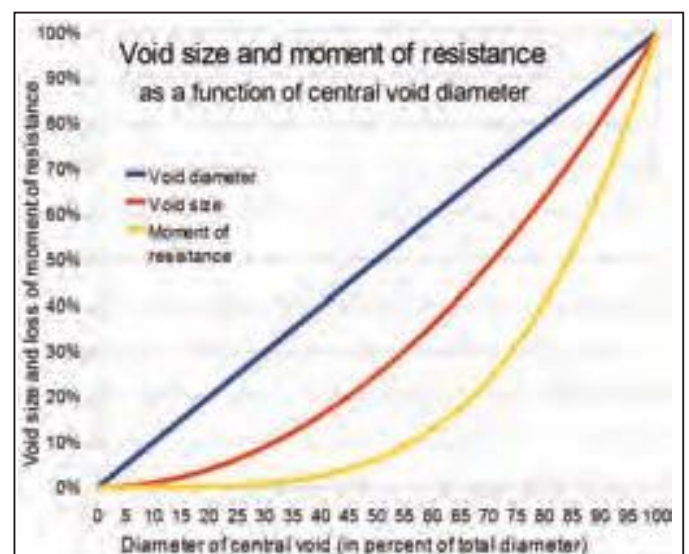


Figure 6. Size of a central cavity and the corresponding relative strength loss as a function of cavity diameter.

Basic Aspects of Mechanical Stability (continued)

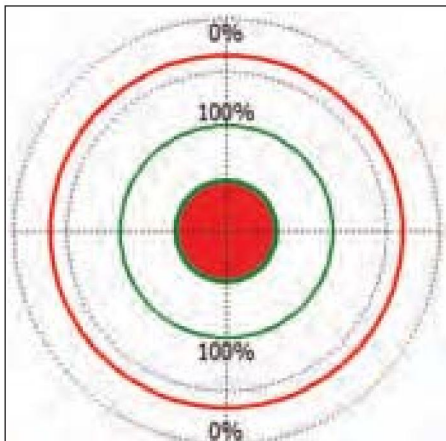


Figure 7. Theoretically, 90 percent loss of radius equals approximately 65 percent loss of moment of resistance.

damaged cross-section for all wind directions. The outward bulge (=relative decrease in stability) on the side opposite from the decay corresponds to the comparatively higher reduction of tensile strength for wind coming from the side where the decay is located.

Therefore, relative strength loss of a trunk cross-section depends not only

on the extent of decay, but also – and above all – on its location. This is relevant for expert assessment of breaking resistance and critical when trying to communicate expert opinion to laymen.

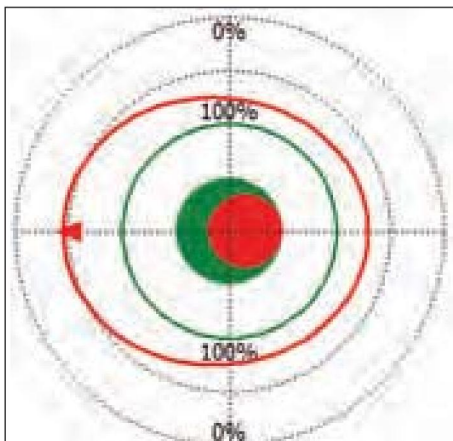


Figure 8. If a cavity covers 50 percent of the cross-section area and is located at the edge, the corresponding relative strength loss is doubled as compared to being located at the center.

Finally, for the real and mostly non-concentric cross-sections of urban trees that have to be inspected, a third curve is calculated in the moment of resistance graph: dividing the values of the red curve (representing the resistance moment of the decayed cross-section) by the green curve (representing the intact cross-section) delivers a curve (in blue)

revealing the relative strength loss in percent for every wind direction. The more the blue curve bulges outward, the higher the strength loss due to wind blowing into this direction.

A typical result is shown in Figure 9, again indicating that decay location is more critical than extent: the blue curve shows that

degradation strongly points towards the south of that trunk cross-section (or bottom of that branch). Even though only about 10 percent of the cross-section area is damaged, the moment of resistance for this direction has already decreased by about 50 percent.

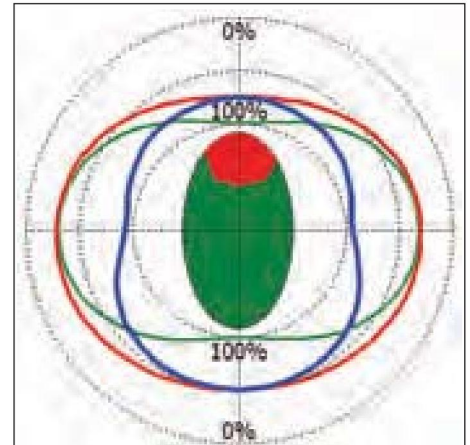


Figure 9. The blue curve reveals the relative strength loss for all load directions due to decay. It is used for evaluating failure potential and as a base for determining risk mitigation strategies, for example a corresponding wind load reduction by pruning.

Summary

The moment of resistance is used to characterize relative strength of cross-sections referring to different static wind loading directions as well as the influence of defects. The first major conclusion is, the cross-section diameter determines a mostly directional stability; the second, that the location of decay is of higher importance than extent. Relative strength loss due to decay can be higher or lower than corresponding loss in cross-section area, strongly depending on cross-sectional shape and defect location. For thin shell walls and dynamic loading, more complex approaches would be required.

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Literature Cited

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Skatter, S., and B. Kucera. 2000. Tree breakage from torsional wind loading due to crown asymmetry. *Forest Ecology and Management* 135(1-3):97-103.

Frank Rinn received his physics diploma from Giessen and Heidelberg University, where his research was on the suitability of resistance drilling for tree-ring analysis in dendrochronology. He holds international patents and trademarks and received 5 innovation awards for developing resistance drilling and sonic tomography. Frank serves as voluntary executive director of ISA Germany and participated in the ISA Biomechanics Week, August 2010.

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Justin Morgenroth and Rien Visser

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